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Techniques for the Statistical Analysis of Observer Data

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ABSTRACT

For vehicle designers, the main goal of experiments on the observability of combat vehicles is a comparison of the probability of detection for two vehicles as a function of range. This paper addresses the statistical techniques to analyze such data to compare the probability of detection of the two vehicles as a function of range. Two techniques are compared: 1. Fitting logistic curves to the data of the vehicles and 2. Using the Fisher Exact Test to compare the probability of detection of the two vehicles at each range. The paper discusses the issues of background variability and confidence levels for hypothesis testing. Finally, a recommendation is made on how to write a specification for the detectability of a vehicle.

1. The Experimental Situation

Consider Figure 1, a sketch of a typical field test of vehicle detectability. Typically, the experimenter offers observers a large number of views of each vehicle at several ranges and in a variety of backgrounds. The experimenter records the numbers of true, false and missed detections of the target vehicle.

Note that in these experiments with fixed observers range cannot be varied independently of background conditions. Figure 2 shows an experimental setup in which range can be varied independently of the background. This setup, however, requires moving the observers as the target remains fixed. Although such a setup could in principal be employed, costs will generally dictate tests with fixed observers.

Such a moveable observer test should generate a monotonic curve of probability of detection (P_d) versus range, Figure 3, because range has varied independently of the vehicle background. On the other hand, a fixed observer test will generate a P_d versus range curve with background variability superimposed on a monotonic curve, Figure 4.

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2. Analysis Techniques

For vehicle designers, the main goal of experiments on the observability of combat vehicles is a comparison of the probability of detection for two vehicles. In this paper, I will compare two techniques for analyzing data from such fixed observer tests:

1. Fitting logistic curves to the data of the vehicles.
2. Using the Fisher Exact Test to compare the probability of detection of the two vehicles at each range.

Logistic Curves

The logistic curve arose from the transformation of probabilities, p , by the so-called logit transformation, namely,

$$y = \log_e \frac{p}{1-p}$$

The logit transformation tends to linearize data in which a proportion is a function of another variable, such as range.

The following equation defines the logistic curve itself:

$$P_d = \frac{1}{1 + b_o(b_{1_i}^R)}$$

General statistics software packages, such as SPSS, can fit a logistic curve to data and can calculate a measure of goodness of fit.

Fisher Exact Test

The Fisher Exact Test is designed to compare two proportions to decide if the proportions are significantly different. The test begins with the preparation of a contingency table. For observer tests, a separate table would be prepared for each range.

For example, consider the following table:

	Vehicle A	Vehicle B	Total
Detect	a	b	a+b
No Detect	c	d	c+d
Total	e	f	e+f
Pd	a/e	b/f	(a+b)/(e+f)

The Fisher Exact Test calculates the probability that the observed contingency table or a more extreme table would be the result of random variations of draws from a population with a Pd of $(a+b)/(e+f)$. The Fisher Exact Test uses the hypergeometric distribution to calculate the required probabilities. The hypergeometric distribution describes the probability, for example, of drawing 5 red cards in a 13-card hand from deck of 26 red and 26 black cards.

The Fisher Exact Test supports direct hypothesis testing. A typical null hypothesis would be that Vehicle A and Vehicle B have the same Pd. The experimenter would select a significance level before the test, for example 5%. If the observed contingency table has a probability less than 5%, then the experimenter can state with greater than 95% confidence that the two vehicles have different Pd's.

3. Discussion

The Fisher Exact Test has advantages over fitting a logistic curve. Because data is compared only at the same range, the effect variability of background with range is avoided. Experimental sample sizes can be calculated for comparison of proportions in order to insure a given difference in Pd will be significant. Moreover, the Fisher Exact Test lends itself to quantitative hypothesis testing.

4. Recommendation on Writing Specifications

The analysis of observer data has a bearing on how specifications should be written. To use quantitative hypothesis tests to judge compliance to specifications, the maximum allowed Pd at given range should be specified instead of the maximum allowed range at Pd of 50%. Consider the following specifications: 1. "The range for a Pd of 50% must be less than R." and 2. "The Pd at a range of R must be less than 50%." The two specifications are equally stringent, but the second specification allows a direct test with a quantitative significance level. On the other hand, the only way to determine the range for Pd of 50% is through interpolation by curve fitting.

Test with Fixed Observers

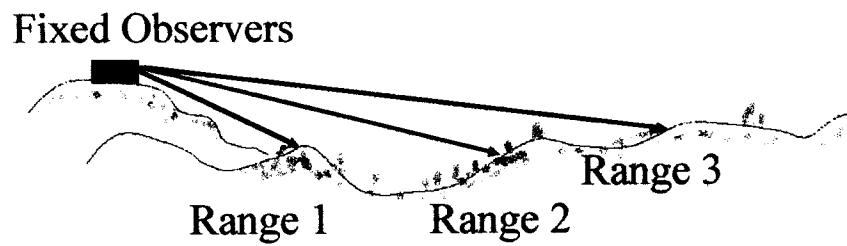


Figure 1. Sketch of an observer test using fixed observers.

Test with Fixed Vehicle

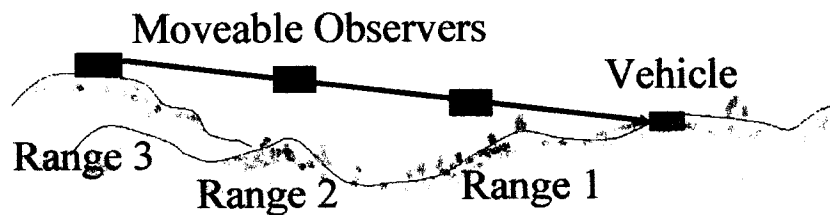


Figure 2. Sketch of an observer test with a fixed target vehicle.

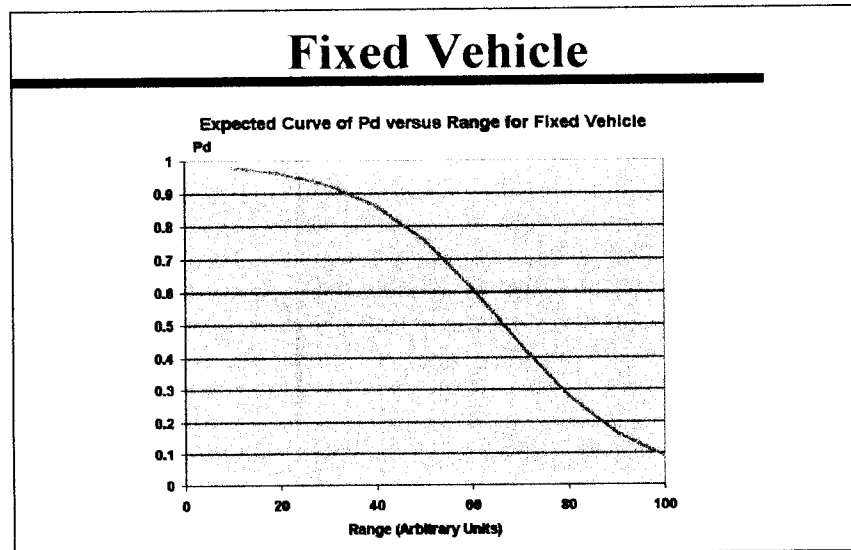


Figure 3. Curve to be expected from a test using a fixed target vehicle.

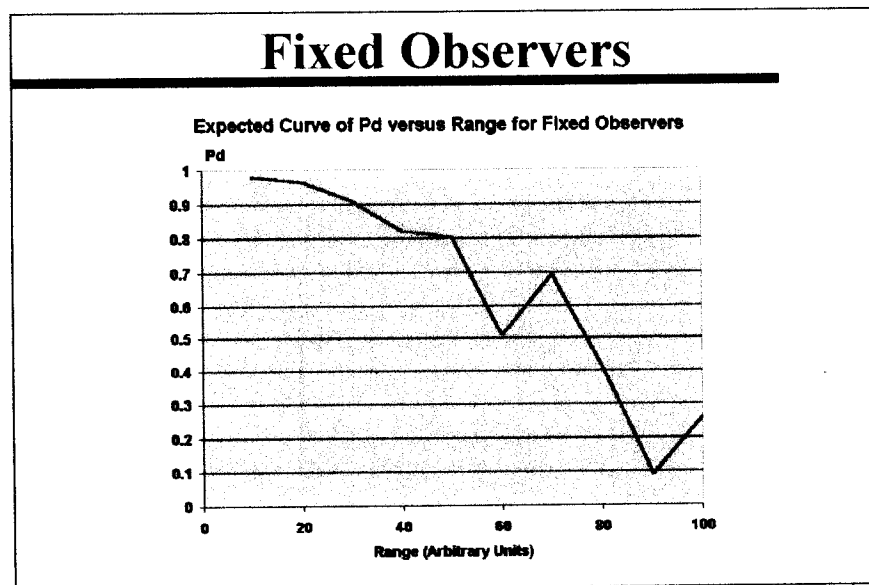


Figure 4. Curve to be expected from an observer test using fixed observers.